

# Isabelle Tutorial:

Truths, Proofs, and Tools

(and how to develop all  
that correctly ...)

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**The ITP Research Programme  
and  
The Evolution of the  
Isabelle/Architecture**

# The “Interactive Proof” Research Programme

- 1968 : Automath
- 1975 : Stanford LCF  
LISP based Goal-Stack, orientation vs.  
functional Programming, Invention:  
Parametric Polymorphism
- 1979 : Edinburgh LCF
- 1984/5 : Cambridge LCF: core LCF principles (1) an abstract  
type of theorems a (2) tactics that deliver a validation in the  
form of a function from a theorem list to a theorem.

## Historic Overviews:

<http://www.cambridge.org/catalogue/catalogue.asp?ISBN=9780521395601>

<http://www.cl.cam.ac.uk/~mjc/papers/HolHistory.pdf>

# The “Interactive Proof” Research Programme

- 1986–88 : HOL88, Isabelle, Coq  
Further search to more foundational and logically safe systems lead to abandon of LCF; HOL became replacement.
  - Invention: Basic Embedding Techniques
  - Invention: Coq: Dependent types, proofobjects
  - Invention: HOL: recursion embeddable, datatype packages, semantics & conservativity
  - Invention: Isabelle: Meta-Logic, tactics as relations over thm's, Meta-Variables, HO Unification, explicit global context (thy's) in thm's and goal's ...

# The “Interactive Proof” Research Programme

- 1990–95 : HOL88, HOL4, Isabelle, Coq,  
Maturing of “classic style”,  
search for more automation
  - Invention: Coq: Powerful Module Systems
  - Invention: HOL: executable “formulas”  
meson-tac, embedding CSP with FP
  - Invention: Isabelle: LF, Cube, FOL, ZF, (HOL)  
higher-order rewriter,  
tableaux prover blast ( 98 ?)

# The “Interactive Proof” Research Programme

- 1995–00 : HOL4, Isabelle, Coq, HOL-light  
Back to more basics again ...  
and more power and framework, too
- Invention: Isabelle: Class-type System,  
proof objects (Isabelle 96 Workshop !!!)  
auto (combined reasoners)
- Invention: Isabelle:  
embedding HOLCF,  
HOL definitively superseded LCF.  
ProofGeneral.

# The “Interactive Proof” Research Programme

- 2000-05 : Isabelle, HOL-light  
Back to more basics again ...  
and more power and framework, too
- Invention: HOL-Light  
Real-number theories & IEEE754,  
Groebner Basis tactics, ...
- Invention: Isabelle:  
ISAR-engine, Proof Documents  
context (state) replaces “theory”  
integration of ATP via Proof Objects

# The “Interactive Proof” Research Programme

- 2005–10 : Isabelle, HOL-light  
Back to more basics again ...  
and more power and framework, too
- Invention: HOL-Light  
Formal Verification of Kernel (without Conservativity)
- Invention: Isabelle: Tools:  
Simpl, HOLCF, HOL-Z,  
TestGen, HOL-OCL, HOL-Boogie,